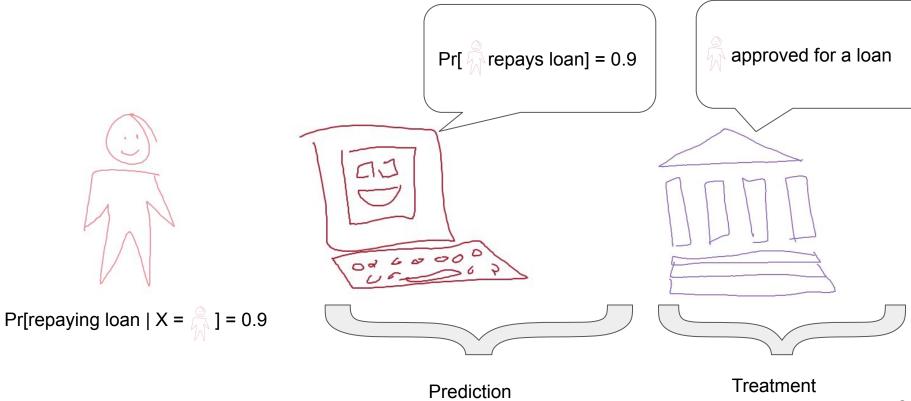
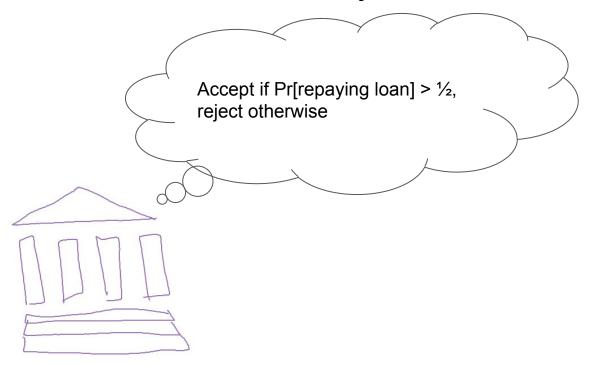
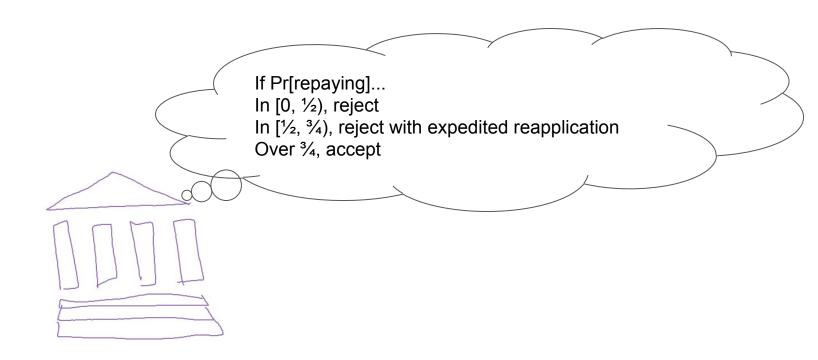
# Visualizing our values: using property elicitation to understand the consequences of constraints

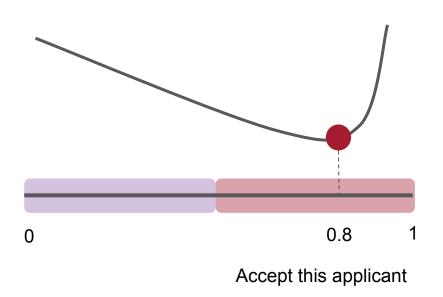
#### Make predictions about people all the time







# Design loss functions to elicit such statistics



Set of outcomes Y	Y = {repay, default}
True p $\in$ ∆ <sub>Y</sub>	p = Pr[repay] = 0.8
Set of predictions U	U = [0,1]
Set of treatments T	T = {award loan, reject loan}

# What happens when we think about the population: adding regularizers

When treatments are individual, simply consider each treatment individually

$$\min_{\vec{u}} L(\vec{u}; \vec{p}) := \frac{1}{m} \sum_{i=1}^{m} L(u_i, p_i)$$

Fairness concerns often merit adding regularizers to losses



$$\min_{\vec{u}} L^{\lambda,R}(\vec{u}; \vec{s}; \vec{p}) := (1 - \lambda) \frac{1}{m} \sum_{i=1}^{m} L(u_i, p_i) + \lambda R(\vec{u}; \vec{s}; \vec{p})$$

Now we need to consider population as a whole, and cannot abstract decisions to the individual level

#### Property elicitation

A loss L <u>elicits</u> a property  $\Gamma$  if, for all  $p \in \Delta^m_{\nu}$ ,

$$\Gamma(\vec{p}) = \arg\min_{\vec{u}} L(\vec{u}; \vec{p})$$

Since L is additive in u, this decomposes into  $\{\Gamma(p_i)\}_i$ 

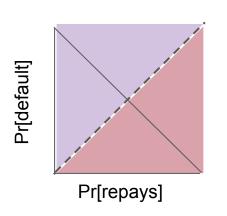
Fix s. A regularized loss elicits a regularized property  $\Theta$  if, for all p in  $\Delta^m_{\ \mathcal{Y}_{,}}$ 

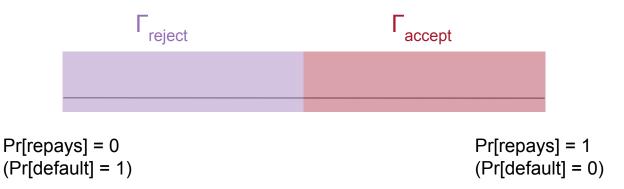
$$\Theta(\vec{p}) = \arg\min_{\vec{u}} L^{\lambda,R}(\vec{u}; \vec{s}; \vec{p})$$

#### Level sets of properties

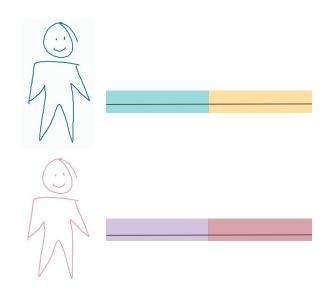
Predictions don't have to be perfect, so long as treatments are correct

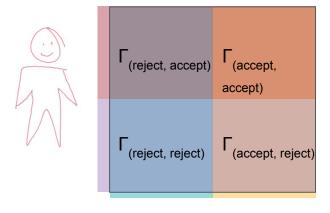
$$\Gamma_t = \{ \vec{p} \in \Delta_{\mathcal{Y}}^m : t \in \Gamma(\vec{p}) \}$$





# Example visualization: 2 agents, binary classification



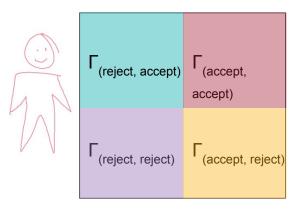


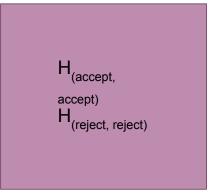


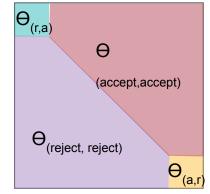
## When do regularizers change the original property?

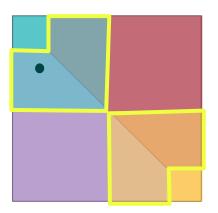
Theorem (informal): Fix  $\lambda \in (0,1)$ . Let L elicit Γ, L<sup>R, $\lambda$ </sup> elicit Θ, and R (which is nonconstant) elicit H. Then  $\Gamma = \Theta$  if and only if  $H = \Gamma$ .

#### Proof by picture: Counterexample with Demographic Parity









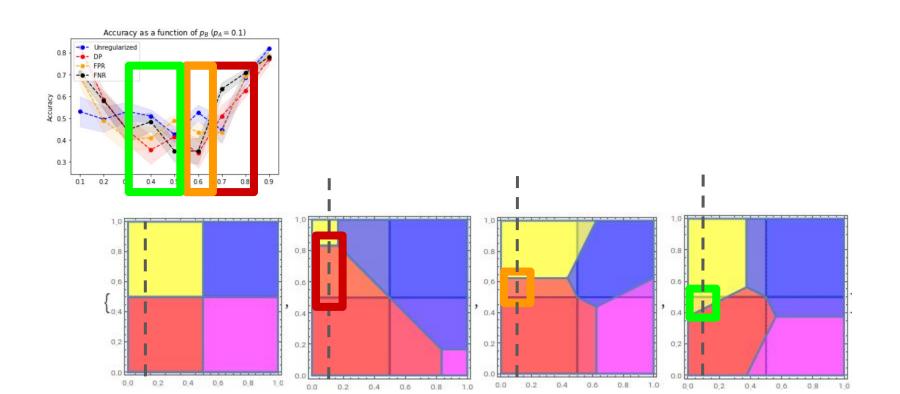


#### Corollary: common group fairness metrics change it up

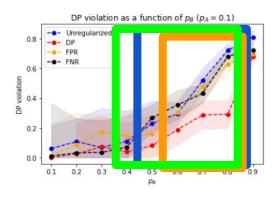
- Most group fairness regularizers change the property
  - They are not additive, so regardless of Γ
- Notable exception: calibration
  - Implies changes imposed by calibration constraints are a result of expressiveness of the model

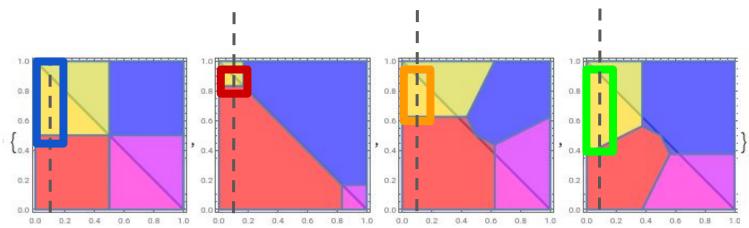


# How decisions change as we go through distribution space



# Fairness violations when regularized





#### In summary, come chat!

- Use high-dimensional property elicitation to study the impacts of different regularizers
  - Examples: group fairness constraints
- Can be used to explain performance gaps and translation across different fairness regularizers

Interested in collaborating, questions?

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# Experimental results

